A Fuzzy Trust Model Using Multiple Evaluation Criteria

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Abstract. This paper is concerned with a fuzzy trust model which takes into account both evaluations from multiple criteria and the recommendations from others in order to set the trust degrees on entities. In the proposed trust model, the entity's preference degrees on the outcomes of the interactions are expressed in fuzzy sets and the trust degrees are determined by aggregating the satisfaction degrees with respect to evaluation criteria with Sugeno's fuzzy integral. In addition, the reputation information is incorporated into the trust degree determination.

1 Introduction

Along with the widespread Internet applications such e-commerce, P2P services and so on, the users have no choice but to take some risks in doing transactions with unknown users or systems over the Internet. In everyday life, we estimate the trust degree on the others by considering the past interaction experience with them and sometimes by referring to the reputation, i.e., word of mouth. In the same token, an on-line entity could reduce the risks to run with the help of the trust information for the interacting entities. Even though there have been proposed various trust models [3-10], there are no models yet generally accepted. Some models are qualitative models^[3] and others are quantitative models^{[4,8-} 10]. Some models depend only on users' ratings to compute the trust value, and others get the trust values by observing the behaviors of the entity over some period. The trust has been defined in various ways because there are no consensus on what constitutes the trust[3-10]. The following is the Gambetta's[6] which is a well-known definition of trust: Trust (or, symmetrically, distrust) is a particular level of the subjective probability with which an agent will perform a particular action, both before [we] can monitor such action (or independently of his capacity of ever to be able to monitor it) and in a context in which it affects

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own action. In the trust models, the following three types of trust are usually considered: situational trust, dispositional trust, and general trust. Situational trust (a.k.a., interpersonal trust) is the trust that an entity has for another entity in a specific situation. Dispositional trust (a.k.a, basic trust) is the dispositional tendency of an entity to trust other entities. General trust is the trust of an entity in another entity regardless of situations. On the meanwhile, the reputation is valuable information for estimating the trust of an entity. The trust of an entity can be differently measured according to which aspects we evaluate. Therefore we propose a trust model to consider multiple evaluation criteria and to enable entities to reflect their preference on the outcomes.

The remainder of this paper is organized as follows: Section 2 briefly presents several related works on the trust models. Section 3 briefly explains the λ -fuzzy measure and the Sugeno's fuzzy integral which are used in the proposed model. Section 4 introduces the proposed fuzzy trust model and Section 5 shows how to apply the model with an example. Finally, Section 6 draws the conclusions.

2 Related Works

Trust and reputation have gained great attention in various fields such as economics, distributed artificial intelligence, agent technology, and so on. Various models for trust and reputation have been suggested as a result[3,4,8-10]. Some models just give theoretical guidelines and others provide computational models.

Abul-Rahman et al. [3] proposed a qualitative trust model where trust degrees are expressed in four levels such as very trustworthy, trustworthy, untrustworthy, and very untrustworthy. The model has somewhat ad-hoc nature in defining the trust degrees and the weights. Azzedin et al. [4] proposed a trust model for a peer-to-peer network computing system, which maintains a recommender network that can be used to obtain references about a target domain. The model is specialized for the well-structured network computing system and thus there are some restrictions on applying the model to general cases. Derbas et al.[8] proposed a model named TRUMMAR which is a reputation- based trust model that mobile agent systems can use in order to protect agents from malicious systems. The model pays special attention to use reputation for trust modeling, but does not consider the multiple evaluation criteria. Shi et al.[9] proposed a trust model which uses the statistical information about the possible outcome distribution for actions. In the model, trust is described as an outcome probability distribution instead of a scalar value. When choosing a candidate, it is used to compute the expected utility value for the candidate entities' actions. Wang et al.[10] proposed a trust model based on Bayesian networks for peer-topeer networks. In the model, a Bayesian network is used to represent the trust between an agent and another agent. Such a Bayesian network represents the probabilities to trust an entity in various aspects. The recommendation values from other entities also are incorporated into the model.

3 Fuzzy Integral for Information Aggregation

The ability of the fuzzy integral to combine the evaluation results from various perspectives has been shown in several works[1,2]. In order to use fuzzy integral for information aggregation, we should have importance degrees assigned to each powerset element of evaluation criteria. These importance degrees are required to preserve the properties of fuzzy measure[1]. The widely used λ -fuzzy measure g_{λ} satisfies the following property along with the fuzzy measure properties[2]: For a finite set $X = \{x_1, x_2, \ldots, x_k\}, g_{\lambda}(\{x_1, \ldots, x_l\}) = \frac{1}{\lambda} \prod_{i=1}^{l} (1 + \lambda g_i) - 1],$ where $g_i = g_{\lambda}(\{x_i\})$.

When all g_i s are given, λ can be derived from the following equation[1]:

$$g_{\lambda}(X) = \frac{1}{\lambda} [\prod_{i=1}^{t} (1 + \lambda g_i) - 1] = 1$$
 (1)

Sugeno's fuzzy integral is a Lebesque integral which has the role of aggregating partial evaluations for an entity in consideration of importance degrees of evaluation criteria[1]. Let X be a set of evaluation items and g(E) the importance degree of evaluation criteria set $E \subset X$ with the properties of fuzzy measure. g(x) denotes the evaluation value on the standpoint of evaluation criterion x, and A denotes the interest focus of evaluation criteria. The Sugeno's fuzzy integral $\oint_A h(x) \circ g(\cdot)$ over the set $A \subset X$ of the function h with respect to a fuzzy measure g is defined as follows:

$$\oint_A h(x) \circ g(\cdot) = \sup_{E \subset X} \{ \min\{ \min_{x \in E} h(x), g(A \cap E) \} \}$$
(2)

$$= \sup_{E \subseteq A} \{ \min\{ \min_{x \in E} h(x), g(E) \} \}$$
(3)

Due to the operation $\min_{x \in E} h(x)$, the fuzzy integral has a tendency to produce pessimistic evaluation. Some decision making problem shows that although an item has poor evaluation, the item can be compensated by other good items. Thus to provide the same effect for the fuzzy integral, we can use a compensatory operator $\psi(\{h(x)|x \in E\})$ instead of the minimum operator in the operation $\min_{x \in E} h(x)$.

4 The Proposed Fuzzy Trust Model

In the literature, there is no consensus on the definition of trust and on what constitutes trust management. In our trust model, however, we take the following definition on the situational trust: Situational trust is the expectation for an entity to provide satisfactory outcomes with respect to the evaluation criteria in a given situation. This section presents how to evaluate the situational trust based on the above definition, how to handle the dispositional trust and the general trust, and how to use recommandation from others and to adjust the recommanders' trust.

4.1 Situational Trust

The situational trust is the trust assigned to an entity for a specific situation. Most existing approaches have interest in how much the considered entity's behaviors are satisfactory[3-10]. It is assumed in their methods to rate the satisfaction degree in a single perspective and it is somewhat ad-hoc on how to rate the satisfaction degrees for an entity to other entities in a specific situation. In the proposed method, the situational trust is estimated as follows: First, an entity α accumulatively constructs the empirical probability distribution of possible outcomes for the interacting entities β with respect to each evaluation criterion in the given situation. Each time the entity α needs to measure the trust in another entity β , she computes the satisfaction degrees with β over each evaluation criterion in the situation. After that, the situational trust of α in β is determined by aggregating the satisfaction degrees in the perspective of evaluation criteria.

Let $TS_{\alpha}(\beta, \delta; EC)$ be the situational trust of entity α in entity β in the situation δ with respect to evaluation criteria $EC = \{ec_1, ec_2, ..., ec_n\}$, where ec_i is an evaluation criterion. It expresses the degree of expectation for trusted entity β to yield satisfactory actions with respect to the evaluation criteria in the given situation. In order to get the situational trust, whenever entity α has an interaction with β , α keeps the records about the evaluation outcomes with respect to the evaluation criteria. The evaluation outcomes are given in either continuous values or categorical attributes. In the case of continuous outcomes, the outcome domain is quantized into several prespecified intervals and outcome values are expressed in the corresponding interval labels.

Empirical Outcome Probability Computation. The entity α 's empirical outcome probability for entity β to make outcome o_i in the situation δ up to time t with respect to an evaluation criterion ec_k is computed as follows:

$$P^{t}(\alpha, \beta, \delta, o_{i}; ec_{k}) = \frac{p^{t}(\alpha, \beta, \delta, o_{i}; ec_{k})}{\sum_{o_{j}} p^{t}(\alpha, \beta, \delta, o_{j}; ec_{k})}$$
(4)

$$p^{t}(\alpha,\beta,\delta,o_{i};ec_{k}) = \rho * \frac{N_{\alpha\beta}^{t}(\delta,o_{i};ec_{k})}{n_{\alpha\beta}} + (1-\rho) * \frac{N_{\alpha\beta}^{[t-dt,t]}(\delta,o_{i};ec_{k})}{n_{\alpha\beta}^{[t-dt,t]}}$$
(5)

In the above equation, $N_{\alpha\beta}^t(\delta, o_i; ec_k)$ indicates the number of outcome o_i for β to produce with respect to ec_k up to time t, $n_{\alpha\beta}$ is the number of total interactions of α with β , $N_{\alpha\beta}^{[t-dt,t]}(\delta, o_i; ec_k)$ is the number of outcome o_i for β to produce with respect to ec_k within the recent time window [t - dt, t], $n_{\alpha\beta}$ is the number of outcome o_i for β to produce with respect to ec_k within the vindow [t - dt, t], $n_{\alpha\beta}$ is the number of outcome o_i for β to produce with respect to ec_k within the window [t - dt, t], and ρ indicates the weighting factor to control the ignorance effect on the past experience.

Satisfaction Degree Computation. The trusting entity α makes her mind on which outcomes are satisfactory for her own preference with respect to each evaluation criterion. For an evaluation criterion ec_i , suppose that its possible outcome is $PO(ec_i) = \{o_{1i}, o_{2i}, ..., o_{ni}\}$. Then, the entity α specifies earlier on her satisfactory outcome set $SO(\alpha, ec_i)$ along with the relative preference for each outcome which is expressed in a fuzzy set as follows: $SO(\alpha, ec_i) =$ $\{(o_1, ow_1), ..., (o_j, ow_j)\}$ where $o_i \in PO(ec_i)$ and $wo_k \in [0, 1]$ is the membership degree to indicate the α 's relative preference to the outcome o_k . The satisfaction degree $SD_{\alpha}(\beta, \delta; ec_i)$ of α with β in the perspective of ec_i is determined as follows:

$$SD_{\alpha}(\beta, \delta; ec_i) = \sum_{(o_k, wo_k) \in SO(\alpha, ec_i)} wo_k \cdot P^t(\alpha, \beta, \delta, o_k; ec_i)$$
(6)

Situational Trust Computation. In the proposed method, the situational trust is measured by the satisfaction degrees of an entity α with other entity β with respect to multiple evaluation criteria EC. For example, when a user determines the trust in a restaurant, she considers her satisfaction degrees for it in the point of her own criteria such as taste of food, waiting time to take a table, availability of her favorite food, and so on. The situational trust of α in β in situation δ with respect to evaluation criteria EC is computed as follows: Here, $\psi(SD_{\alpha}(\beta, \delta; A))$ is the value obtained after the application of a compensatory operator to the situational trust values $SD_{\alpha}(\beta, \delta; ec_i)$ for $ec_i \in A$, and WC(A) is the relative importance that α weighs for the evaluation criteria set A.

$$TS_{\alpha}(\beta,\delta;EC) = \oint_{EC} SD_{\alpha}(\beta,\delta;\cdot) \circ WC(\cdot) = \sup_{A \subset EC} \min\{\psi(SD_{\alpha}(\beta,\delta;A)), WC(A)\}$$
(7)

4.2 Dispositional Trust

The dispositional trust TD_{α} represents the dispositional tendency for a trusting entity α to trust other entities. Each entity is supposed to assign her own dispositional trust value. It could be used as the initial general trust when an entity starts an interaction with a new entity.

4.3 General Trust

The general trust $TG_{\alpha}(\beta)$ of entity α in entity β is the trust that α has on β regardless of situations. It plays the role of the initial situational trust for β in a new situation. It can be used as the reputation weight for β at the beginning. It can be also used as the situational trust value while enough interactions have not yet made. The general trust of α in β is obtained by averaging the situational trusts for the experienced situations Φ as follows:

$$TG_{\alpha}(\beta) = \frac{\sum_{\delta \in \Phi} TS_{\alpha}(\beta, \delta; EC)}{|\Phi|}$$
(8)

4.4 Reputation

When an entity decides whether it starts an interaction with another entity, it is valuable to refer to available reputation information about the entity. A reputation is an expectation about an entity's behavior which is formed by the community having interacted with the entity based on the information about or the observations of its past behaviors. When the recommenders γ_j are available for an entity β in a situation δ , the entity α might take into account the recommendations for β . Each entity could have different preference on the outcomes with respect to the evaluation criteria and thus it is not so meaningful to directly use the trust values for β from the recommenders γ_j . Therefore we take the approach to take the recommender γ_j 's empirical outcome probabilities $P^t(\gamma_j, \beta, \delta, o_k; ec_i)$ for β instead of γ_j 's trust value $TS_{\gamma_j}(\beta, \delta; EC)$ on β . With the received outcome probabilities, the satisfaction degrees $SD^r_{\gamma_j}(\beta, \delta; ec_i)$ from γ_j are computed as follows: Here wo_k^{α} is the preference degree of the entity α for the outcome o_k .

$$SD^{r}_{\gamma_{j}}(\beta,\delta;ec_{i}) = \sum_{o_{k}\in SO(\alpha,ec_{i})} wo^{\alpha}_{k} \cdot P^{t}(\gamma_{j},\beta,\delta,o_{k};ec_{i})$$
(9)

Then the situational trust value $TS^r_{\gamma_j}(\beta, \delta; EC)$ from the recommender γ_j is computed as follows: Here $\psi(SD^r_{\gamma_j}(\beta, \delta; A))$ is the value obtained by the application of a compensatory operator to the satisfaction degrees $SD^r_{\gamma_j}(\beta, \delta, ec_k)$ for $ec_k \in A$ from γ_j , and WC(A) is the relative importance that α weighs for the evaluation criteria set A.

$$TS^{r}_{\gamma_{j}}(\beta,\delta;EC) = \oint_{EC} SD^{r}_{\gamma_{j}}(\beta,\delta;\cdot) \circ WC(\cdot) = \sup_{A \subset EC} \min\{\psi(SD^{r}_{\gamma_{j}}(\beta,\delta;A)), WC(A)\}$$
(10)

The reputation value $TR_{\alpha}(\beta, \delta; EC)$ of β for α is computed by taking the weighted sum of the situational trust $TS_{\gamma_j}^r(\beta, \delta; EC)$ from recommenders γ_j as follows: Here the weighting factor wr_j is the recommendation trust value for the recommender γ_j . That is, wr_j is the degree to which α believes the recommendation from γ_j . These weights are updated through the interaction with the entities.

$$TR_{\alpha}(\beta, \delta; EC) = \frac{\sum_{j} wr_{j} \cdot TS_{\gamma_{j}}^{r}(\beta, \delta; EC)}{\sum_{j} wr_{j}}$$
(11)

4.5 Combination of Situational Trust and Reputation

When an entity starts to work in a community, she assigns her own dispositional trust value. The dispositional trust is used as the initial general trust when she interacts with an entity for the first time. Until sufficient number of interactions has made for a given situation, the general trust is used as the situational trust. Once the situational trust $TS_{\alpha}(\beta, \delta; EC)$ and the reputation $TR_{\alpha}(\beta, \delta; EC)$ are obtained, the final trust value $TS_{\alpha}(\beta, \delta; EC)$ is computed by their weighted aggregation as follow: Here, w is the relative weighting factor for the situational trust, $w \in [0, 1]$.

$$TS_{\alpha}(\beta, \delta; EC) = w \cdot TS_{\alpha}(\beta, \delta; EC) + (1 - w) \cdot TR_{\alpha}(\beta, \delta; EC)$$
(12)

4.6 Update of the Recommender Trust

The recommender's trust wr_i is updated according to how much their recommendation score is close to the final computed trust value $TS_{\alpha}(\beta, \delta; EC)$. If

the recommendation score is similar to the final trust value, the recommender's recommendation trust is increased by a small amount. Otherwise, the recommender's recommendation trust is decreased by an exponential factor term. The following shows the update rule for the recommender trust wr_i .

Let $\Delta = |TS_{\alpha}(\beta, \delta; EC) - TS_{\gamma_i}^r(\beta, \delta; EC)|$. If $\Delta < \epsilon$, $wr_i(t+1) = \min\{wr_i(t) \cdot (1+\eta), 1\}$ where ϵ and η are small values such that $0 \leq \epsilon, \eta \leq 1$. Otherwise, $wr_i(t+1) = wr_i(t)(1-e^{-\lambda\Delta})$ where λ is a small value such that $0 \leq \lambda \leq 1$.

5 An Application Example

In order to show how the proposed model works, the section gives an example to apply the model. Suppose that an entity P_1 has interest in the trust of a restaurant R_1 in terms of $EC = \{ \text{taste } ts, \text{ waiting time } wt, \text{ favorite food availability } fa \}$ with the help of the recommenders P_2 and P_3 . Suppose that the satisfying outcome sets of P_1 for EC are given in the following fuzzy sets:

 $SO(ts) = \{ (bad bd, 0), (moderate md, 0.5), (good gd, 0.7), (excellent ex, 1) \}$ $SO(wt) = \{ ([0,15] t_1, 1), ((15,30] t_2, 0.7), ((30,50] t_3, 0.5), ((50, \infty) t_4, 0) \}$ $SO(fa) = \{ (available av, 1), (not available na, 0) \}$

Let the situation δ be going out to the restaurant R_1 on the weekends. Suppose that the empirical outcome probability distributions $P^t(P_i, R_1, \delta, o_i; ec_k)$ are given as in Table 1:

	O_i									
	taste ts			waiting time wt			e wt	availability fa		
	bd	md	gd	ex	t_1	t_2	t_3	t_4	av	na
$P^t(P_1, R_1, \delta, o_i; EC)$	0	0.2	0.3	0.5	0.7	0.1	0.2	0	0.6	0.4
$P^t(P_2, R_1, \delta, o_i; EC)$	0.2	0.2	0.5	0.1	0.4	0.5	0.1	0	0.5	0.5
$P^t(P_3, R_1, \delta, o_i; EC)$	0	0.1	0.2	0.7	0.3	0.4	0.2	0.1	0.7	0.3

Table 1. The empirical outcome probability distributions

Computation of the Trust. Then the satisfaction degree of P_1 and the satisfaction degrees from P_2 and P_3 in perspective of P_1 is obtained using Eq.(6) and Eq.(9) respectively, as in Table 2.

Table 2.	The	satisfaction	degrees
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	ec_i				
	taste ts	waiting time wt	availability fa		
$SD_{P_1}(R_1,\delta;ec_i)$	0.84	0.87	0.6		
$SD_{P_2}^r(R_1,\delta;ec_i)$	0.6	0.8	0.5		
$SD_{P_3}^{r}(R_1,\delta;ec_i)$		0.68	0.7		

Suppose that the relative importance degrees for the evaluation criteria are given as 0.5, 0.3, and 0.2 to ts, wt, and fa, respectively, and the importance degrees satisfy the properties of the λ -fuzzy measure. From Eq.(9), we can get a parameter λ of the λ -fuzzy measure satisfying $0.06\lambda^2 + 0.47\lambda + 0.2 = 0$. The unique root greater than -1 for this equation is $\lambda = -0.45$ which produces the following fuzzy measure on the power set of EC.

subset A of EC	$g_{-0.45}(A)$
ϕ	0
$\{ts\}$	0.5
$\{wt\}$	0.3
$\{fa\}$	0.4
$\{ts, wt\}$	0.87
$\{wt, fa\}$	0.75
$\{fa, ts\}$	0.99
$\{ts, wt, fa\}$	1

For Eq.(7), let us use the compensatory operator $\psi(A) = \tau \cdot \min_{x_i \in A} \{x_i\} + (1-\tau) \cdot \max_{x_i \in A} \{x_i\}$ where $\tau = 0.4$. Then the situational trust $TS_{P_1}(R_1, \delta; EC)$ of P_1 in R_1 is computed by Eq.(7) as follows:

 $TS_{P_1}(R_1, \delta; EC) = \sup_{A \subset EC} \min\{\psi(SD_{P_1}(R_1, \delta; A)), WC(A)\} \\ = \sup\{\min\{0.84, 0.5\}, \min\{0.6, 0.3\}, \min\{0.91, 0.4\}, \min\{0.744, 0.87\}, \\ \min\{0.786, 0.75\}, \min\{0.882, 0.99\}, \min\{0.84, 1\}\} = 0.882$

The situational trusts $TS_{P_i}^r(R_1, \delta; EC)$ from the recommenders P_2 and P_3 are computed by Eq.(10) as follows:

 $TS_{P_2}^r(R_1, \delta; EC) = 0.89 \qquad TS_{P_2}^r(R_1, \delta; EC) = 0.80$

If the recommender trust values wr_{P_i} for P_2 and P_3 are 0.8 and 0.7, respectively, then the reputation of R_1 for P_1 is computed as follows:

$$TR_{P_1}(R_1, \delta; EC) = (0.8 * 0.89 + 0.7 * 0.80)/(0.8 + 0.7) = 0.837$$

If the weighting factor w for the situation trust is 0.7, then the final trust value $TS_{P_1}(R_1, \delta; EC)$ is computed by Eq.(12) as follows:

$$TS_{P_1}(R_1, \delta; EC) = 0.7 * 0.882 + 0.3 * 0.837 = 0.867$$

Based on this trust value, the entity P_1 would decide whether to do business with the entity R_1 .

6 Conclusions

The trust information for the online entities are valuable in reducing the risks to take on doing some transactions. We proposed a fuzzy trust model which has the following characteristics: The model allows to look at entity's trust in the point of multiple evaluation criteria. It maintains the empirical outcome distributions for evaluation criteria and enables the trusting entities to express their fuzzy preference on the outcomes when estimating trust in other entities. In addition, the model makes it possible for the entities to put different weights on the evaluation criteria, which are aggregated by using Sugeno's fuzzy integral. When it makes use of the recommendations from others, it takes the outcome distributions instead of their recommending trust values. Thereby, it allows to reflect the trusting entity's preference and her own weighting on the evaluation criteria in the evaluation of the recommendation.

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